

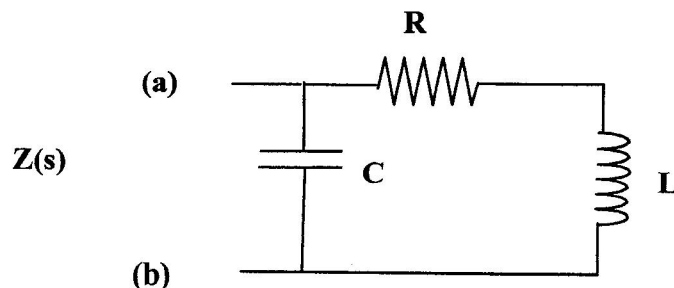
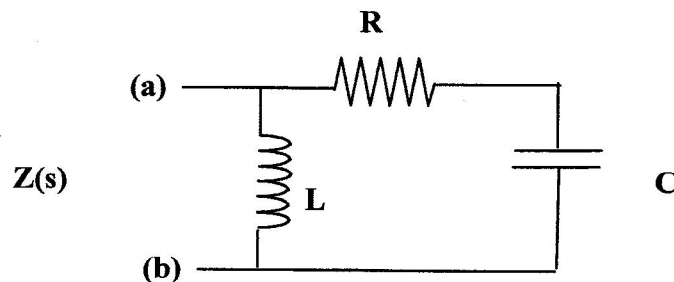
**EP311 Fall Term 2005**  
**Final Exam (50% of total course grade)**

**6 problems, all equal weight**

**Problem 1: Generalized Impedances**

Write the generalized impedances  $Z(s)$  presented between the terminals (a) and (b) of the 2 circuits shown below. Arrange the expression for  $Z(s)$  such that you have polynomials in increasing powers of  $s$  in both the numerator and denominator.

Sketch on the s-plane the poles and zeros in each case. Note that you may assume that component values have been chosen such that  $\left(\frac{R}{2L}\right)^2 < \frac{1}{LC}$



## Problem 2: Semiconductor Physics

The portion of the periodic table most important for semiconductor work is reproduced below

Group III	Group IV	Group V
Boron (B) Z=5	Carbon (C) Z=6	Nitrogen (N) Z=7
Aluminum (Al) Z=13	Silicon (Si) Z=14	Phosphorus (P) Z=15
Gallium (Ga) Z=31	Germanium (Ge) Z=32	Arsenic (As) Z=33
Indium (In) Z=49	Tin (Sn) Z=50	Antimony (Sb) Z=51

- A silicon sample is doped with Boron such that  $N(B)/N(Si) = 10^{-6}$ . What type of doping is this? What is the electrical conductivity?
- The same sample is now doped with Arsenic to the ~~same concentration~~, i.e.  $N(As)/N(Si) = 5 \times 10^{-7}$ . What type of doping does this produce? What is the conductivity now?
- Compare the conductivities of the two doped samples. Which is higher, and why?

### Additional Useful Information

Physical Parameters for Silicon:

$$\begin{aligned} \text{Atomic concentration} \\ N(Si) = 5.0 \times 10^{22} \text{ cm}^{-3} \end{aligned}$$

$$\begin{aligned} n_i &= 1.5 \times 10^{10} \text{ cm}^{-3} \\ \mu_e &= 1350 \text{ cm}^2/\text{V.s} \\ \mu_h &= 480 \text{ cm}^2/\text{V.s} \end{aligned}$$

Recall also  $\sigma = e(n_e \mu_e + n_h \mu_h)$  { $e$  = electron charge =  $1.6 \times 10^{-19}$  Coulomb}

- At room temperature (assume 25 degrees C) the current in a silicon diode is measured to be 200 mA at a forward bias voltage of 0.7 Volt. What is the reverse leakage current for this diode? What current would flow at a forward bias of 0.6 Volt?

Ref: Shockley equation  $I = I_0 [e^{(eV/\eta kT)} - 1]$  ( $\eta \approx 1$  and  $k = 1.38 \times 10^{-23}$  J/K)

### Problem 3: Bipolar Junction Transistor (BJT)

(a) In the circuit given below the Bipolar Junction Transistor Q1 has the following parameters at room temperature (assume 25 °C):

$$\beta = 100$$

$$I_{CBO} = 100 \text{ pA.}$$

Given the following changes in parameters as a function of temperature:

$$\Delta V_{BE} = -2.5 \text{ mV/}^\circ\text{C}$$

$I_{CBO}$  doubles for every 10 °C rise in temperature

$\beta$  increases from 100 to 200 when the temperature increases by 50 °C

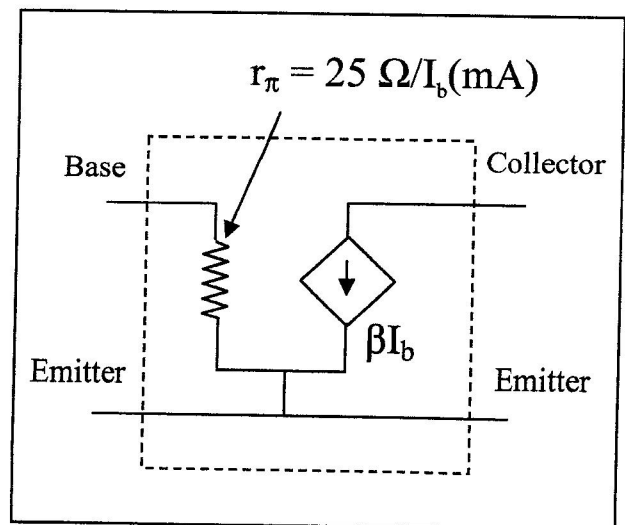
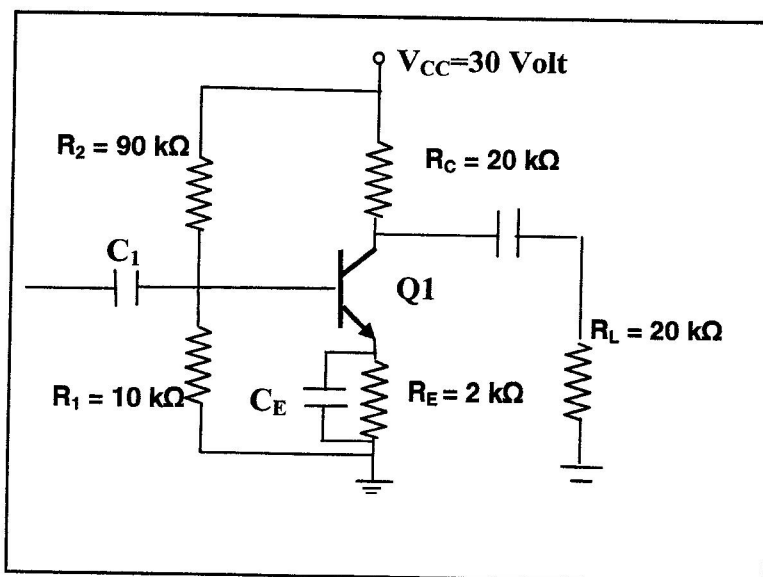
Use the standard BJT bias stability equation (given) to calculate the change in collector current due to a

$$50^\circ\text{C rise in temperature: } I_C = \frac{V_{BB} - V_{BE} + (1 + \frac{1}{\beta}) I_{CBO} (R_B + R_E)}{R_E + \frac{R_B + R_E}{\beta}}$$

(Recall that  $R_B$  is the parallel combination of the base bias resistors  $R_1$  and  $R_2$ , i.e.  $R_B = R_1 // R_2$ )

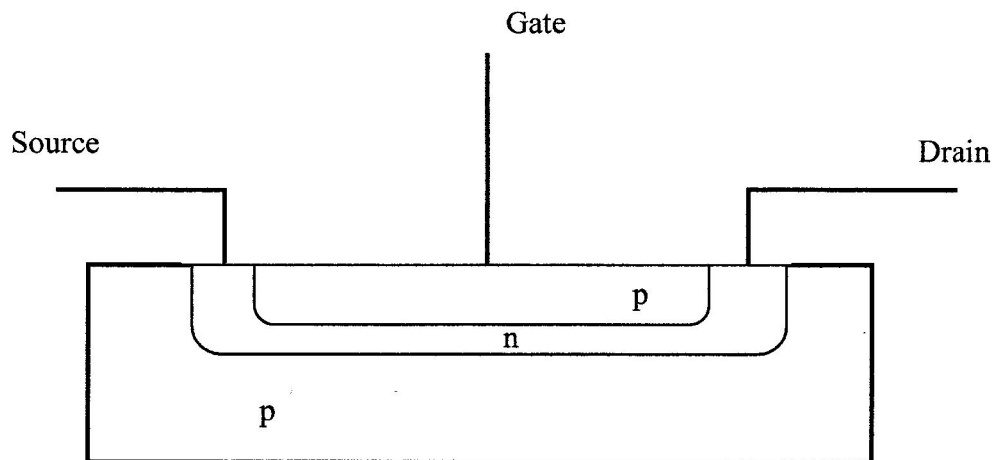
(b) If the lowest desired frequency of operation is 2 kHz, choose capacitors  $C_1$ ,  $C_2$ , and  $C_E$

(c) Draw the AC equivalent circuit assuming the capacitors have been chosen correctly and that  $V_{CC}$  is an AC ground. Then replace the transistor by the  $r_\pi - \beta$  model of the transistor shown in the figure and calculate the voltage gain (Remember the emitter is AC-shorted to ground if the  $C_E$  capacitor is properly chosen)



**Problem 4: JFET Circuit**

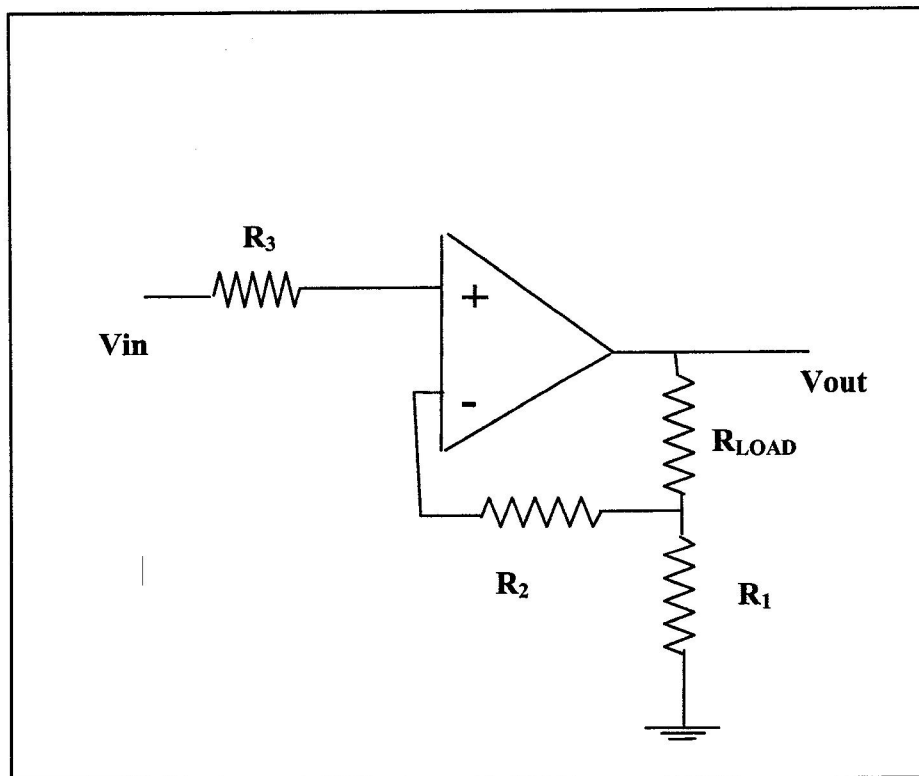
- (a) Explain qualitatively how the following n-channel JFET works. Sketch a circuit showing the proper biasing for this device
- (b) What is the circuit symbol for this device, and why is it drawn the way it is ?
- (c) Why do we never forward bias the gate channel junction ?
- (d) What is the chief advantage of a JFET over a BJT ?



**Problem 5: Op-amp DC Current Source**

Use the op-amp current and voltage rules (OACR and OAVR) to find the expression for the current through the load resistor  $R_{LOAD}$  in terms of the input voltage  $V_{in}$  for the circuit below.

Describe the function of this op-amp circuit in words.



**Problem 6: Op-amp AC Circuit – Effective Inductance using Capacitors & Feedback**

- (a) Derive the relationship between  $V_{in}(\omega)$  and  $I_{in}(\omega)$  for the following op-amp circuit by using the op-amp current and voltage rules (OACR, OAVR).
- (b) What is the effective inductance of this circuit ?
- (c) Why is this not a true inductor simulator ?

